

# Sound level recommendations for quiet sonic boom dose-response community surveys

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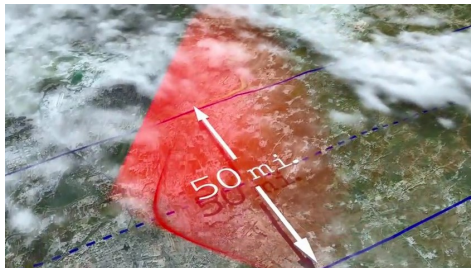
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**NC STATE**  
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# Background

- ▶ Traditional sonic booms are loud and startling
- ▶ Sonic booms can be heard up to 25 miles on either side of the flight path along the entire supersonic route



- ▶ In 1973, the FAA banned commercial overland supersonic flights
- ▶ What if sonic booms could be quiet enough to be publicly acceptable?

# Motivation

- ▶ NASA has a two step plan:
  1. Make sonic booms as quiet as a thump by changing shape of aircraft
  2. Work with noise regulators to replace supersonic ban with a supersonic noise limit
  
- ▶ To determine the noise limit, we need to understand the relationship between noise levels and how communities react
  
- ▶ In order to do so, we need to conduct multiple community surveys for data collection

## Motivation (continued)

- ▶ The Low Boom Flight Demonstration aircraft (LBFD) is designed for quiet supersonic flight and expected to be complete in 2020's

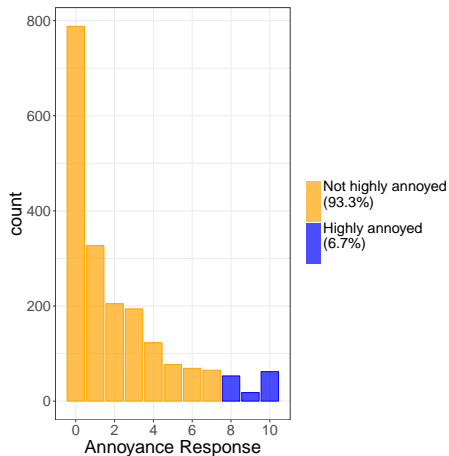


- ▶ Data from a 2011 pilot study is used to develop methods and analysis techniques
  - ▶ Quiet low-booms were created from an F-18 dive maneuver

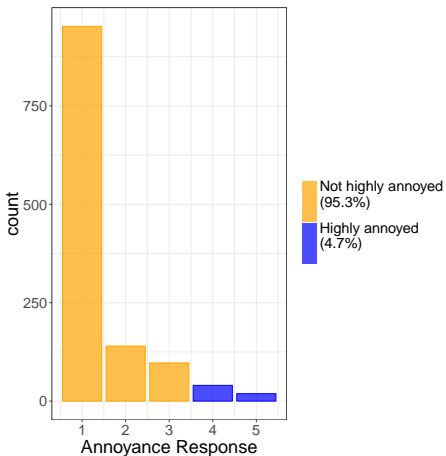
# Data

- ▶ Panel data because each respondent responded multiple times
- ▶ Over a two-week period, with a total of 110 booms
- ▶ Combine two data subsets with different response scales
- ▶ Data validation
  - ▶ Reproduce results from analysis reports
  - ▶ We found some minor discrepancies but for methods development purposes, they are negligible

# Data Summary



(a) 11-point scale survey



(b) 5-point scale survey

- ▶ Total of 97 respondents and 3229 responses
- ▶ Noise level range of sonic booms: 63-106 PLdB

# Research Goals

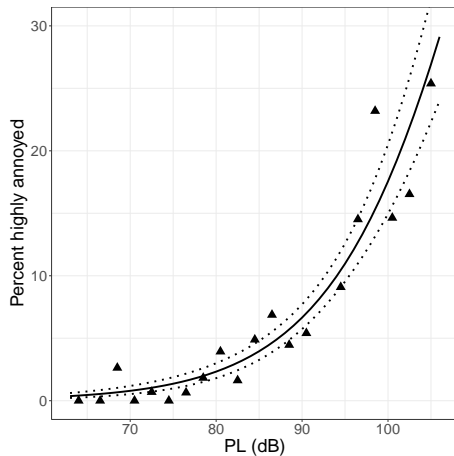
- ▶ Model the relationship between noise levels and percent highly annoyed as a dose-response relationship
- ▶ We expect a limited noise level range that the LBFD can achieve (i.e., [70, 80] PLdB)
- ▶ Research question: what are the implications of testing in a limited range of noise levels?

# Logistic Regression

- ▶ A common model for dose-response relationship
- ▶ Explanatory variable: sound metric Perceived Level (PL) in dB
- ▶ Response variable: binary response  $Y_i$  where
$$Y_i = \begin{cases} 1 & \text{if respondent is highly annoyed} \\ 0 & \text{otherwise} \end{cases}$$
- ▶ Let the probability of highly annoyed at  $PL_i$  be  $p_i$
- ▶  $Y_i \sim \text{Bernoulli}(p_i)$ , where  $p_i = \text{logit}^{-1}(\beta_0 + \beta_1 PL_i) = \frac{e^{\beta_0 + \beta_1 PL_i}}{1 + e^{\beta_0 + \beta_1 PL_i}}$
- ▶ Quantities of interest include:
  - ▶ Estimates and confidence intervals for percent highly annoyed given PLdB
  - ▶ Estimates and confidence intervals for PLdB given percent highly annoyed

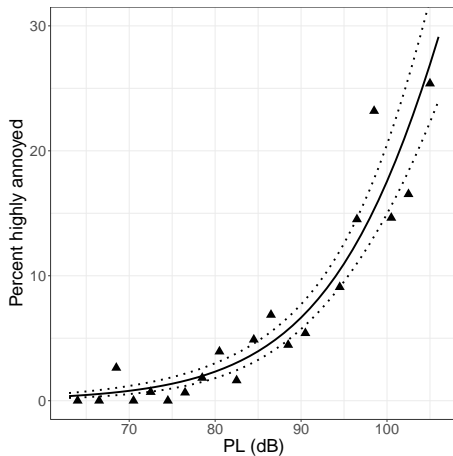


# Results

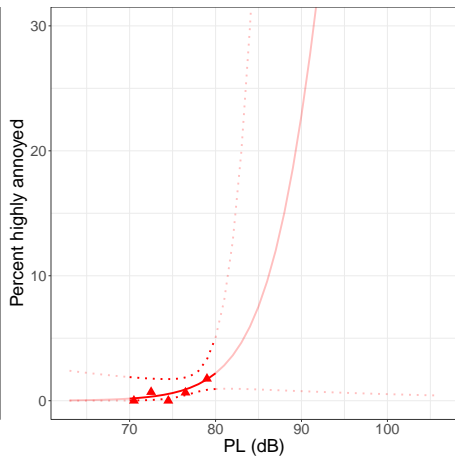


(a) Full range fit

## Results



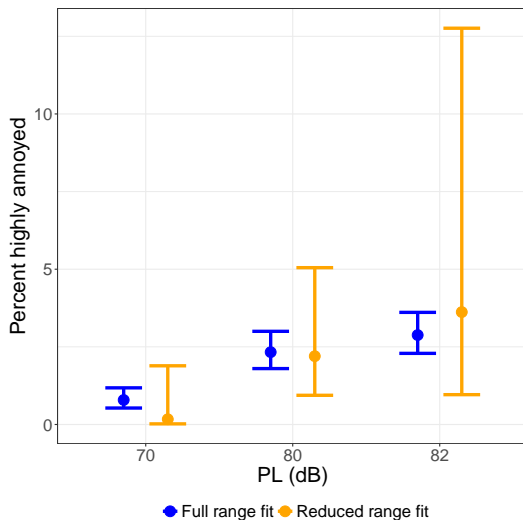
(a) Full range fit



(b) Reduced range fit

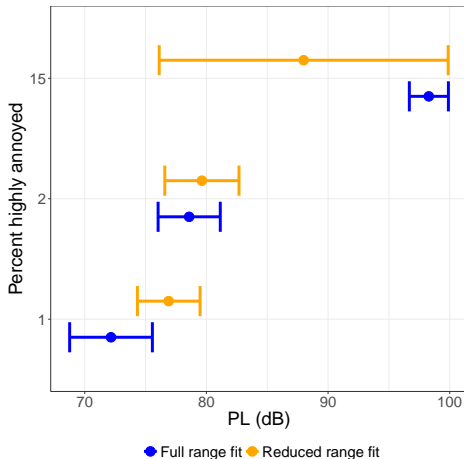
# Estimates of quantities of interest

- ▶ Percent highly annoyed given PL



# Estimates of quantities of interest (continued)

- ▶ PL given percent highly annoyed
  - ▶ Confidence intervals are calculated using Delta Method <sup>1</sup>



<sup>1</sup>Casella & Berger (2002)

# Conclusions

- ▶ For reduced range fit:
  - ▶ estimated quantities within reduced range data have higher precision,
  - ▶ extrapolated quantities beyond reduced range have high uncertainty
- ▶ For Lbfd tests, if the range tested does not include the future noise limit, estimates will have high uncertainty

# Continuing work

- ▶ Evaluate and compare candidate models
- ▶ Logistic regression model assumes:
  - ▶ probability of highly annoyed,  $p_i$ , for every individual is the same, and
  - ▶ independence in  $Y_i$ , ignoring longitudinal nature of data
- ▶ Other candidate models:
  - ▶ multilevel models<sup>2</sup> to take into account of different individuals' probability of high annoyance
  - ▶ first-principles based model<sup>3</sup> from psychoacoustics literature
- ▶ How many responses (observations) are necessary for LBFD surveys?

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<sup>2</sup>Groothuis-Oudshoorn & Miedema (2006)

<sup>3</sup>Fidell et al. (2011)

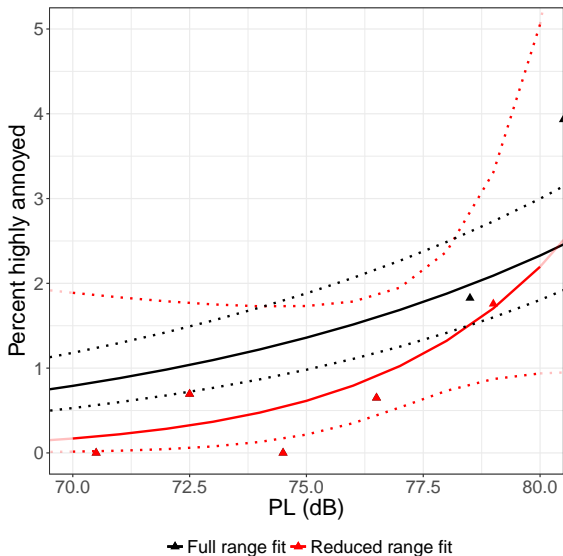
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# Backup



# Results



# Comparison of estimates and confidence intervals

- ▶ Percent highly annoyed given PL
  - ▶ Confidence intervals for reduced range are about two times wider than those for full range

PL (dB)	Estimates (%)	Conf. Intervals
70	0.79	(0.53, 1.18)
75	1.36	(0.98, 1.88)
80	2.33	(1.80, 3.00)

Table 1: Estimates for full range fit

PL (dB)	Estimates (%)	Conf. Intervals
70	0.17	(0.02, 1.89)
75	0.61	(0.22, 1.73)
80	2.2	(0.94, 5.05)

Table 2: Estimates for reduced range fit

## Comparison of estimates and confidence intervals (continued)

- ▶ PL given percent highly annoyed
  - ▶ Confidence intervals are calculated using Delta Method <sup>4</sup>

Perc. HA	Estimates	Conf. Intervals
0.5	65.79	(61.50, 70.07)
1	72.16	(68.76, 75.56)
2	78.58	(76.03, 81.14)

Table 3: Estimates for full range fit

Perc. HA	Estimates	Conf. Intervals
0.5	74.2	(69.35, 79.05)
1	76.9	(74.33, 79.48)
2	79.63	(76.58, 82.68)

Table 4: Estimates for reduced range fit

<sup>4</sup>Casella & Berger (2002)